

FUNCTIONS TEST – 3º ESO

Exercise 1: (1.25 points) Work out the domain of the following functions:

a) $f(x) = \frac{1}{x^2 - 9}$

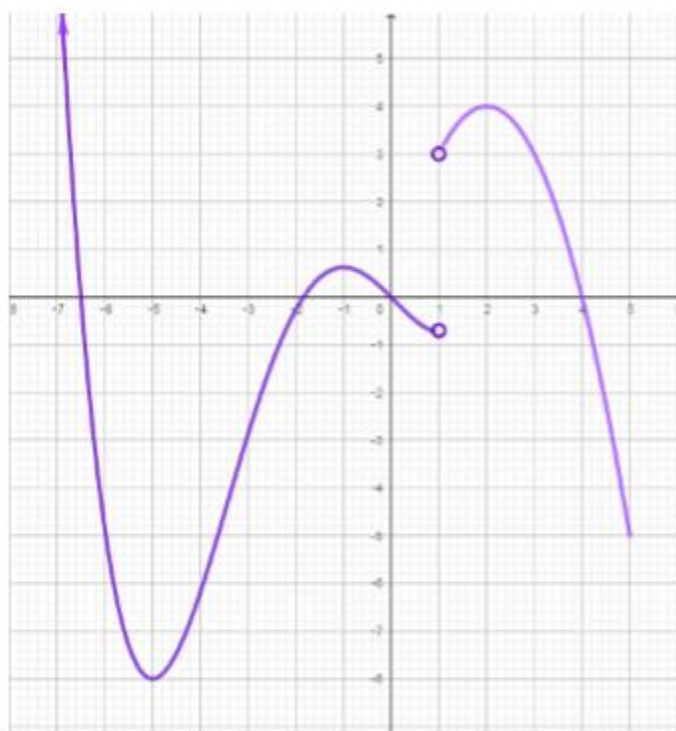
b) $f(x) = \sqrt[3]{x^2 - 5x + 6}$

c) $f(x) = \sqrt{x+5}$

Exercise 2: (1 point) Plot the graph of a function that fulfills all the following characteristics at the same time:

- a) Its domain is $[-5, 7]$
- b) It crosses the axes at the points $(-2, 0)$, $(0, 3)$ and $(5, 0)$
- c) It has maxima at $x = -1$ and $x = 3$ and a minimum at $x = 0$, either local or global

Exercise 3: (1.75 points) Given the following graph of a certain function:



- a) Indicate its domain and its image. Is it a continuous function?
- b) Determine the points where the function crosses the axes
- c) Study its monotony
- d) Study the relative and absolute extrema

Exercise 4: (2.5 points)

- a) Find the slope and the y-intercept of the straight line $3x + 4y - 5 = 0$
- b) Work out the **general** equation of the straight line that passes through the points $P(2, -1)$ and $Q(5, 1)$
- c) Work out the equation of the straight line that is parallel to $5x + y - 9 = 0$ and passes through the point $A(2, -3)$.

Exercise 5: (1.5 points) Plot the graph of the function $f(x) = 9 - x^2$, indicating its direction, studying the points where it crosses the axes and finding the coordinates of the vertex.

Exercise 6: (2 points) Plot the graph of the piecewise function given below

$$f(x) = \begin{cases} 3x + 8 & x \leq -2 \\ 2 & -2 < x \leq 1 \\ x^2 - 6x + 5 & 1 < x < 6 \end{cases}$$